

# AML 883 Properties and selection of engineering materials

## **LECTURE 8. Plasticity**

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# Problem Sheet 3

Problems on strength-limited design are up on the homepage.

# Hardness

Resistance of a material to plastic deformation,  
measured usually by indentation

# Measuring hardness

- Mohs → Historical interest
  - Brinell → Macro tests
  - Rockwell → Macro tests
  - Vickers → Micro tests
  - Knoop → Micro tests
  - Nanoindentation
- 
- ```
graph LR; Mohs --> HI[Historical interest]; Brinell --> MT[Macro tests]; Rockwell --> MT; Vickers --> Micro[Micro tests]; Knoop --> Micro; Nanoindentation;
```

# Mohs scale

- Very ancient
- Idea is simple – Softest material that can scratch the given material or the hardest mineral on which the given material can produce a scratch
- It is really just a way of ordering
- All the images in the following ten slides are courtesy: wiki

# Mohs scale 1

- Talc



# Mohs scale 2

- Gypsum



# Mohs scale 3

- Calcite





# Mohs scale 4

- Fluorite



# Mohs scale 5

- Apatite



# Mohs scale 6

- Feldspar



# Mohs scale 7

- Quartz



# Mohs scale 8

- Topaz



# Mohs scale 9

- Corundum

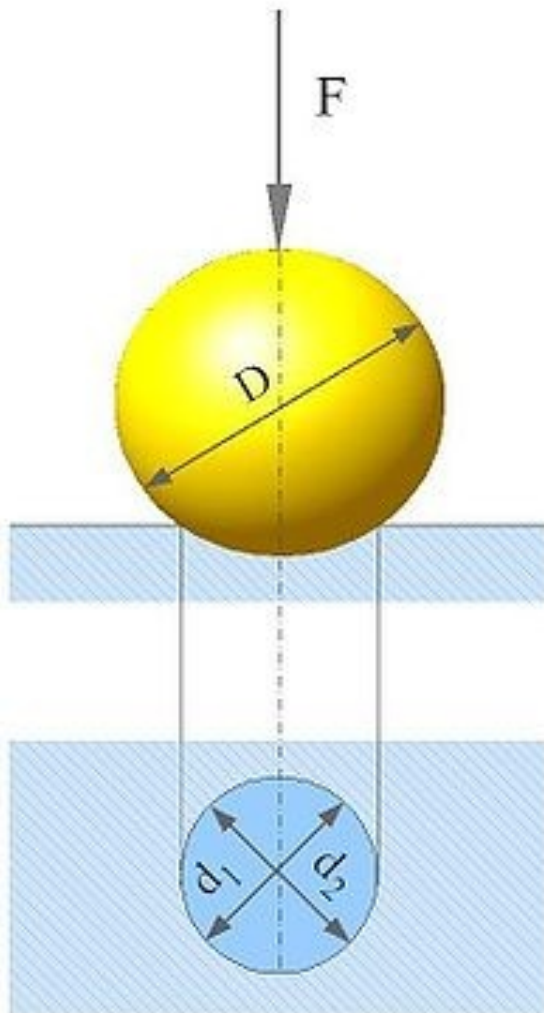


# Mohs scale 10

- Diamond



# Brinell hardness tester



- 10 mm dia steel ball
- 29 kN force (3000 kgf)
- Softer – less force
- Harder – Tungsten carbide ball
- Image courtesy: wiki



# Brinell hardness number

- Using the formula

$$BHN = 2P / \pi D (D - (D^2 - d^2)^{1/2})$$

- “d” -- indentation diameter (mm)
- “P” -- force in kgf
- “D” -- indenter diameter (mm)

# Rockwell hardness tester

- Brinell is not truly non-destructive test
- Rockwell – a minor load and then a major load; note the depth of penetration; read the hardness on a dial
- Indentor – cone or sphere

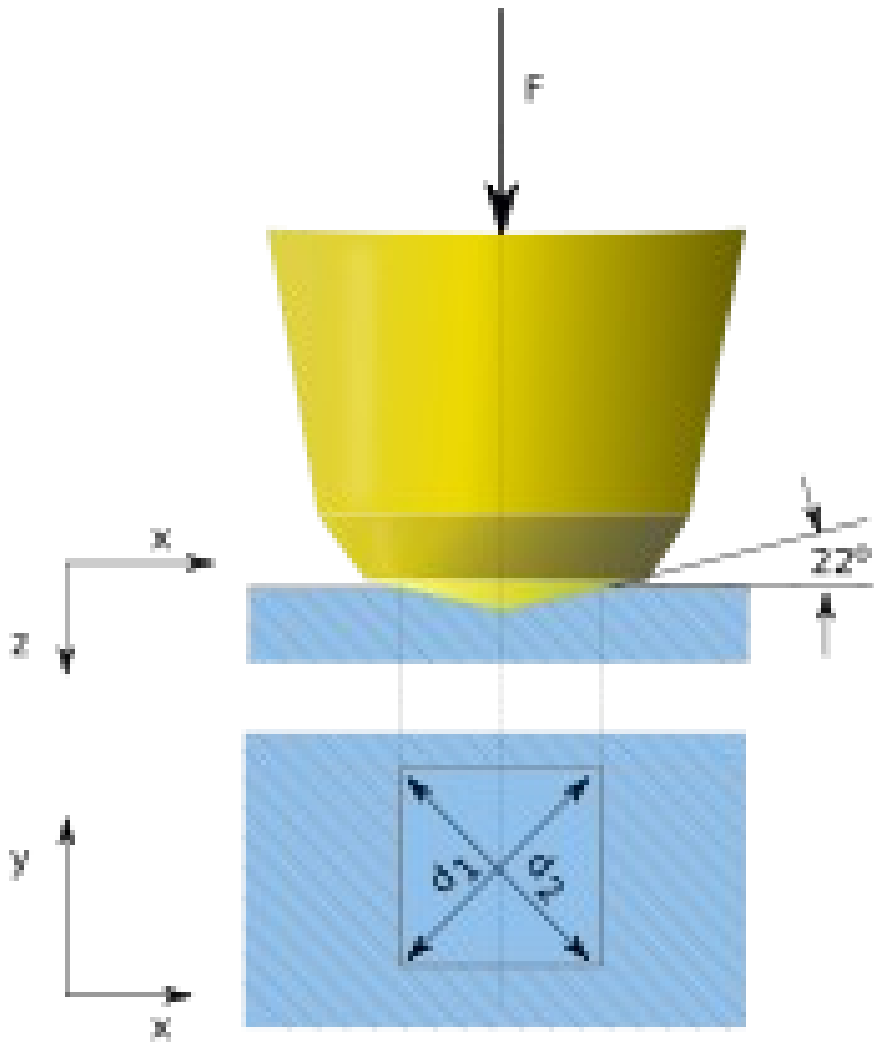
# Vickers hardness test



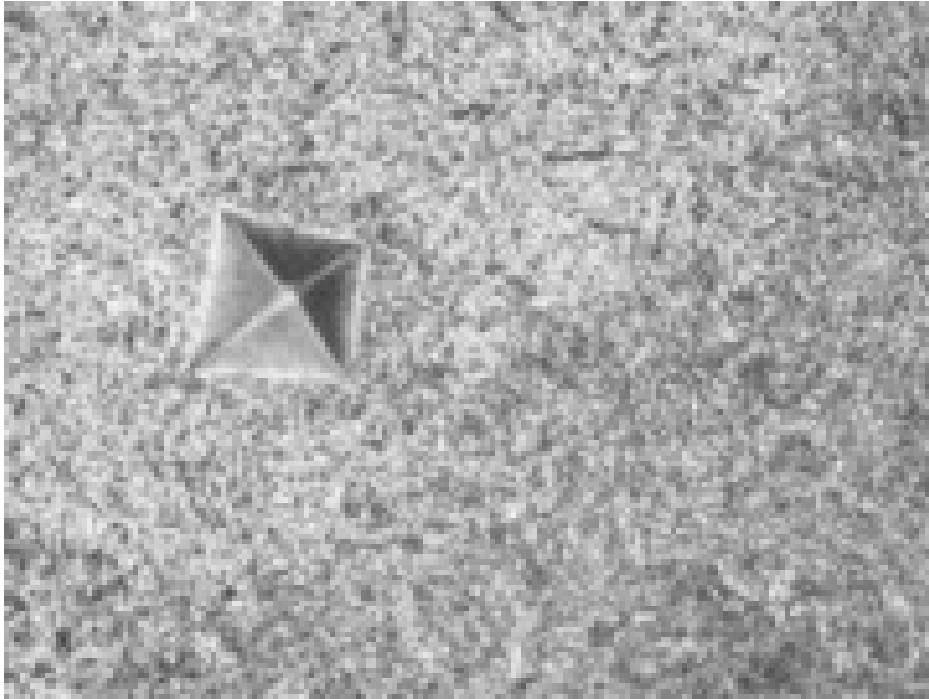
- Vickers hardness tester
- Vickers pyramid number (HV)
- Square based pyramidal diamond indenter
- Image courtesy:wiki

# Vickers hardness test

- Area measurement
- $H = F/A$
- Image courtesy:wiki



# Vickers hardness test

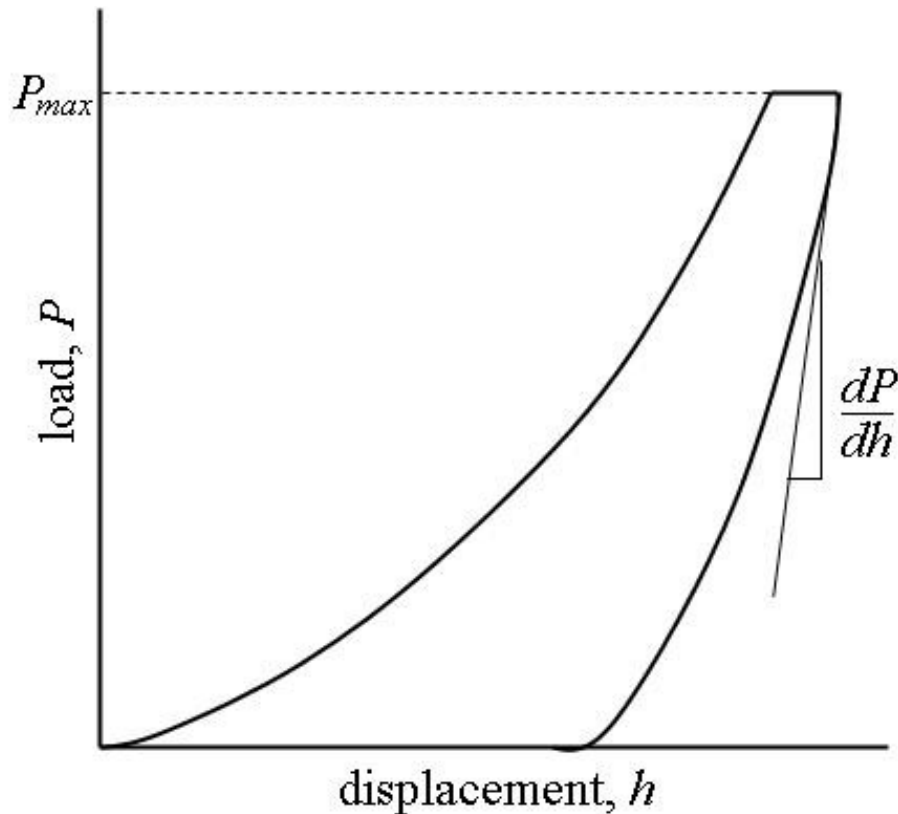


- Indentation on hardened steel
- Area measurement
- $H = F/A$
- Image courtesy:wiki

# Knoop hardness test

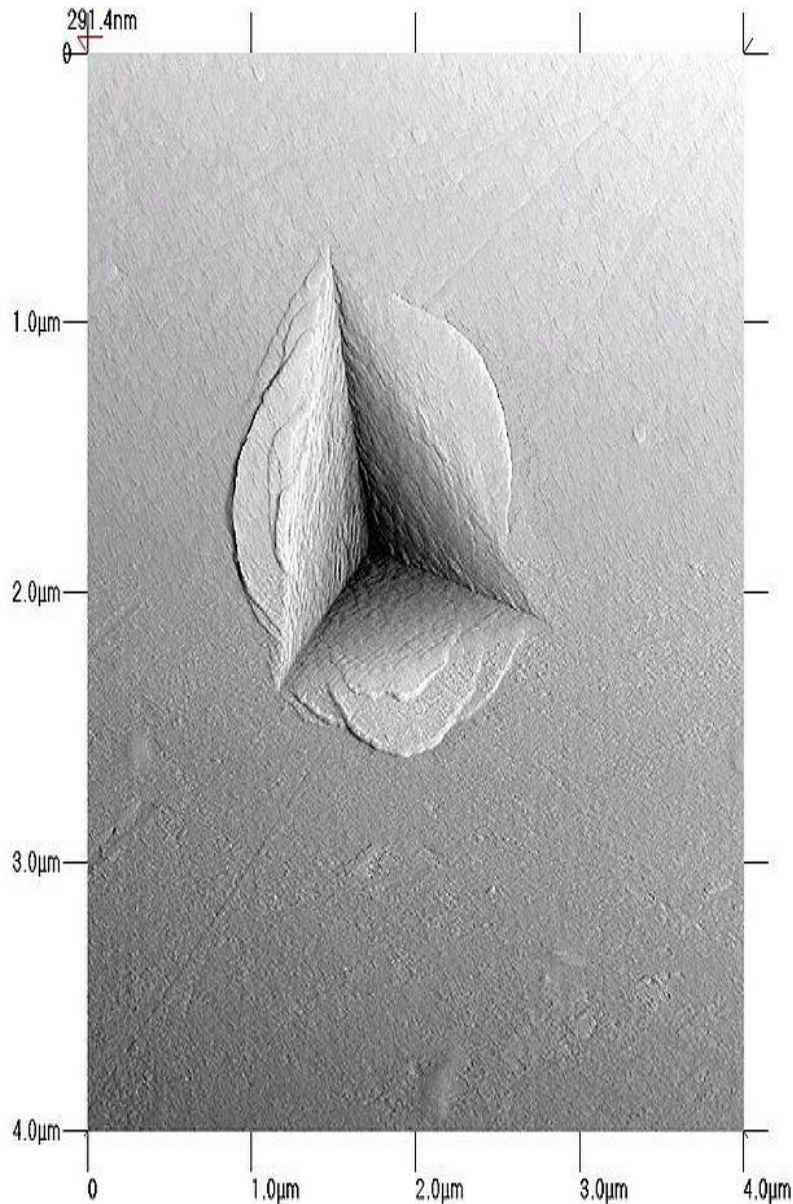
- For very brittle materials and thin sheets
- Requires a microscope to measure the indentation
- Pyramidal diamond point – press on surface!

# Nanoindentation



- Load versus displacement from an instrumented nanoindenter
- Image courtesy: wiki

# Nanoindentation



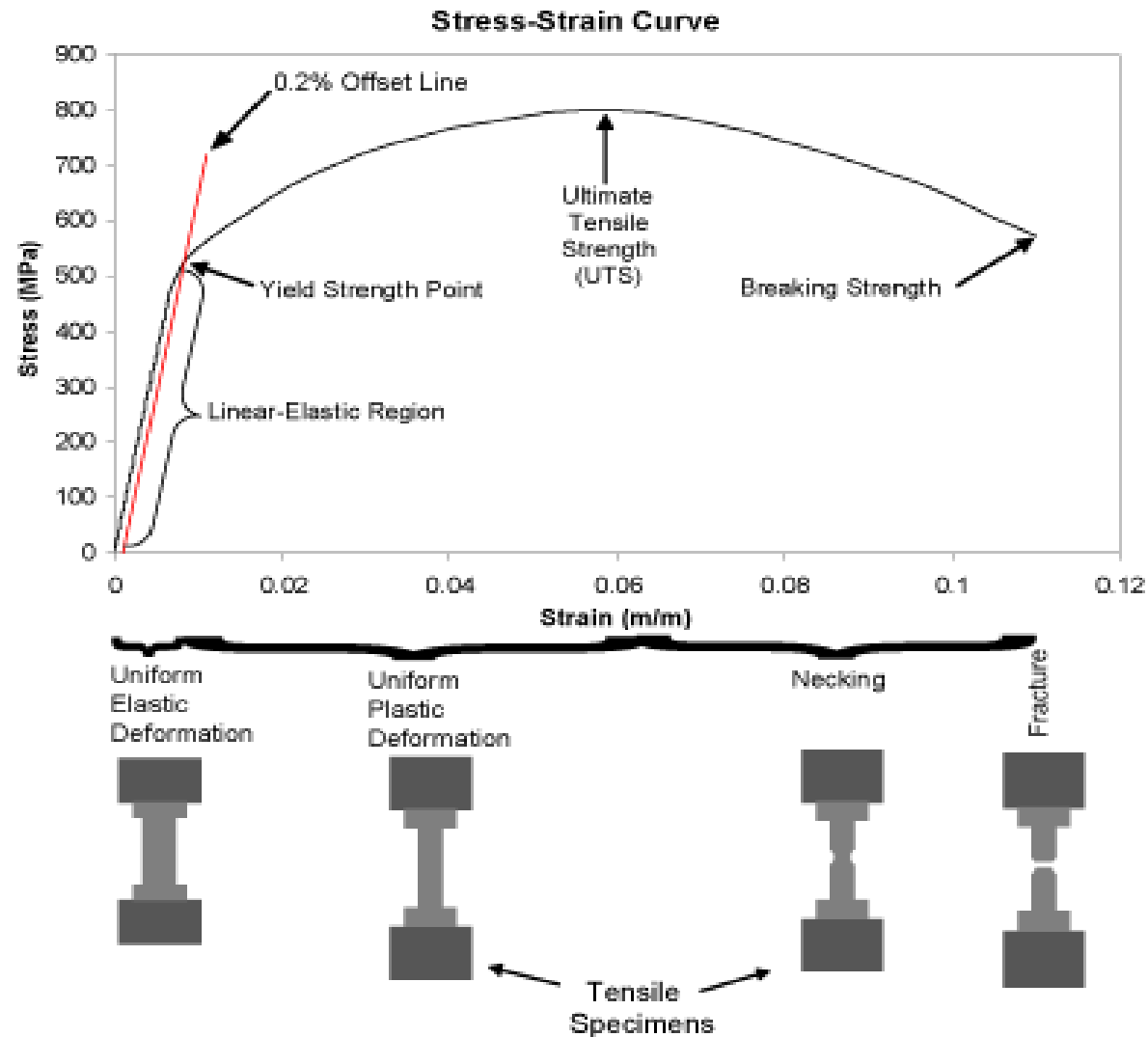
- AFM image of nanoindentation in Zr-Cu-Al metallic glass
- Berkovich indenter – triangular pyramid
- Image courtesy: wiki



# Hardness to yield strength

- Vickers – one third of yield strength
- Other hardness numbers – can similarly be converted
- Information from hardness tests – less accurate and less complete
- Not used for design

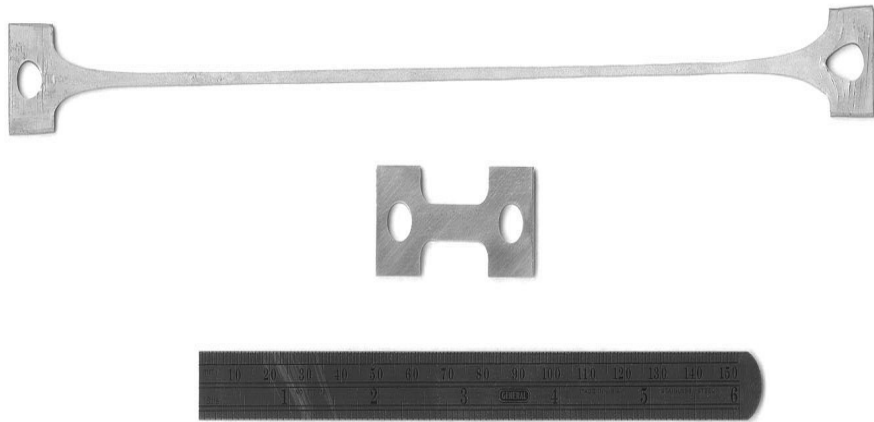
# Stress-strain curve



# Plastic strain

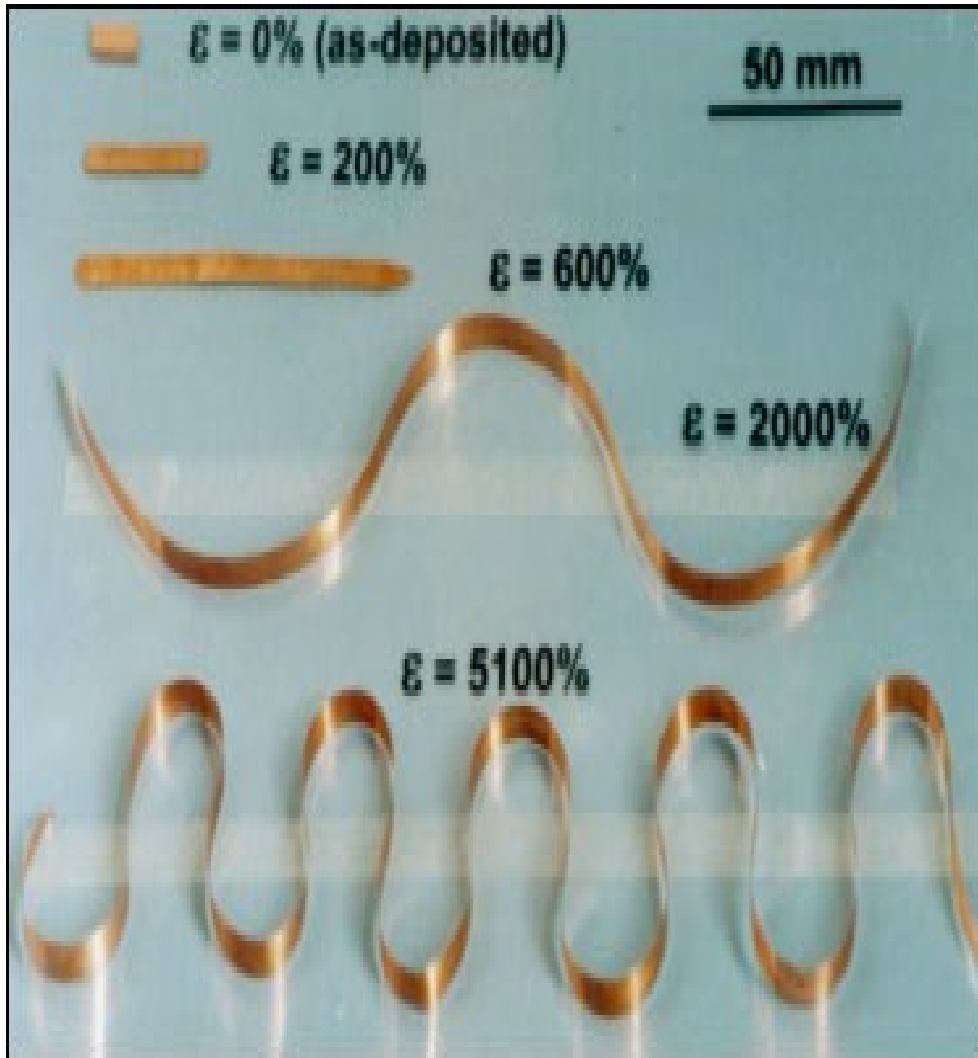
- By definition, permanent strain resulting from plasticity
- Total strain – elastic strain
- Plastic work – area under the stress-strain curve in the plastic regime
- Ductility – how much plastic strain can a material take
- Super-ductile materials -- superplastic!

# Superplasticity



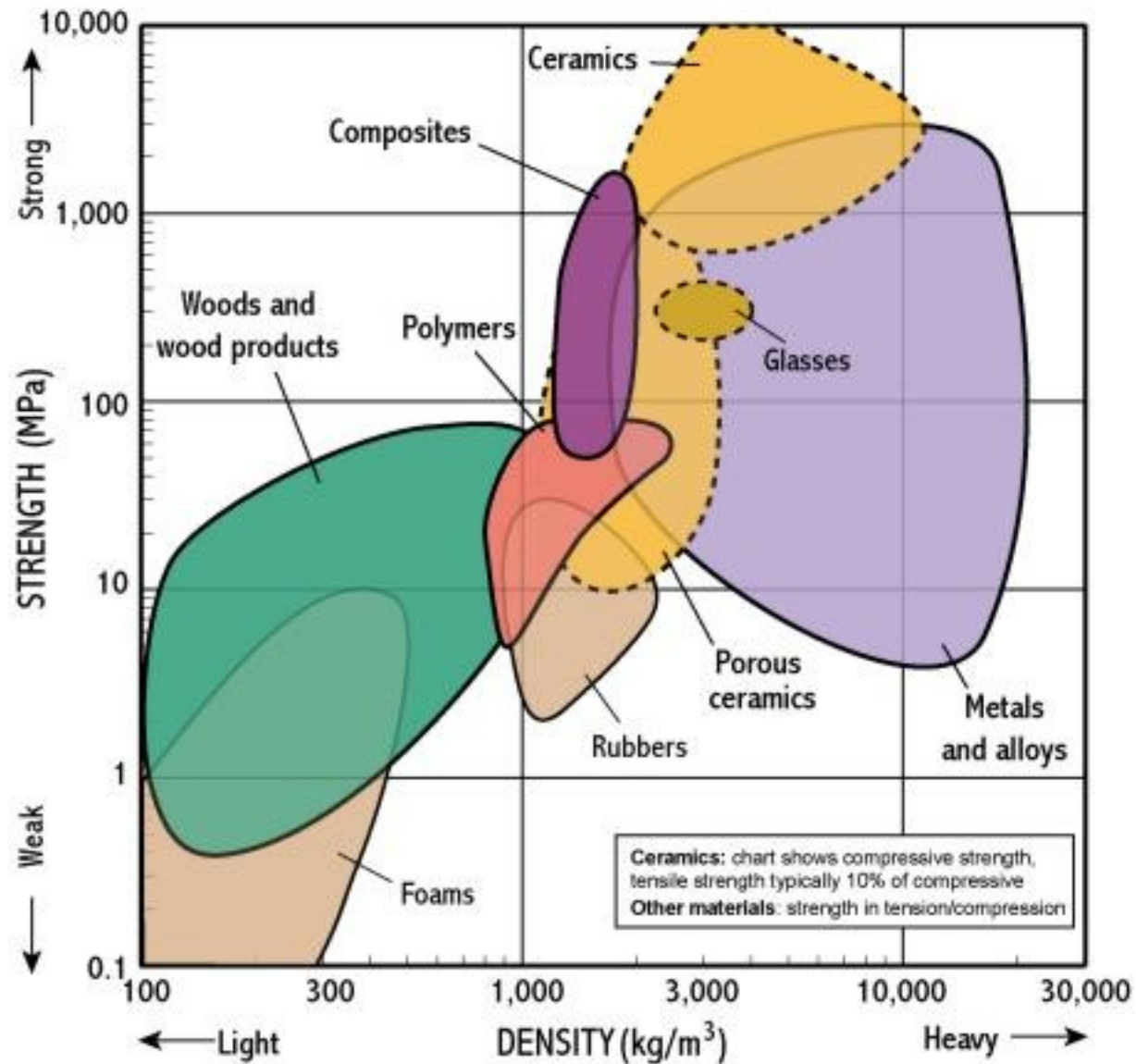
- Deformation amounting to 1000% or even more (8000% is the largest reported?)
- UCDavis, ChemEngg-MatSci site

# Superplasticity

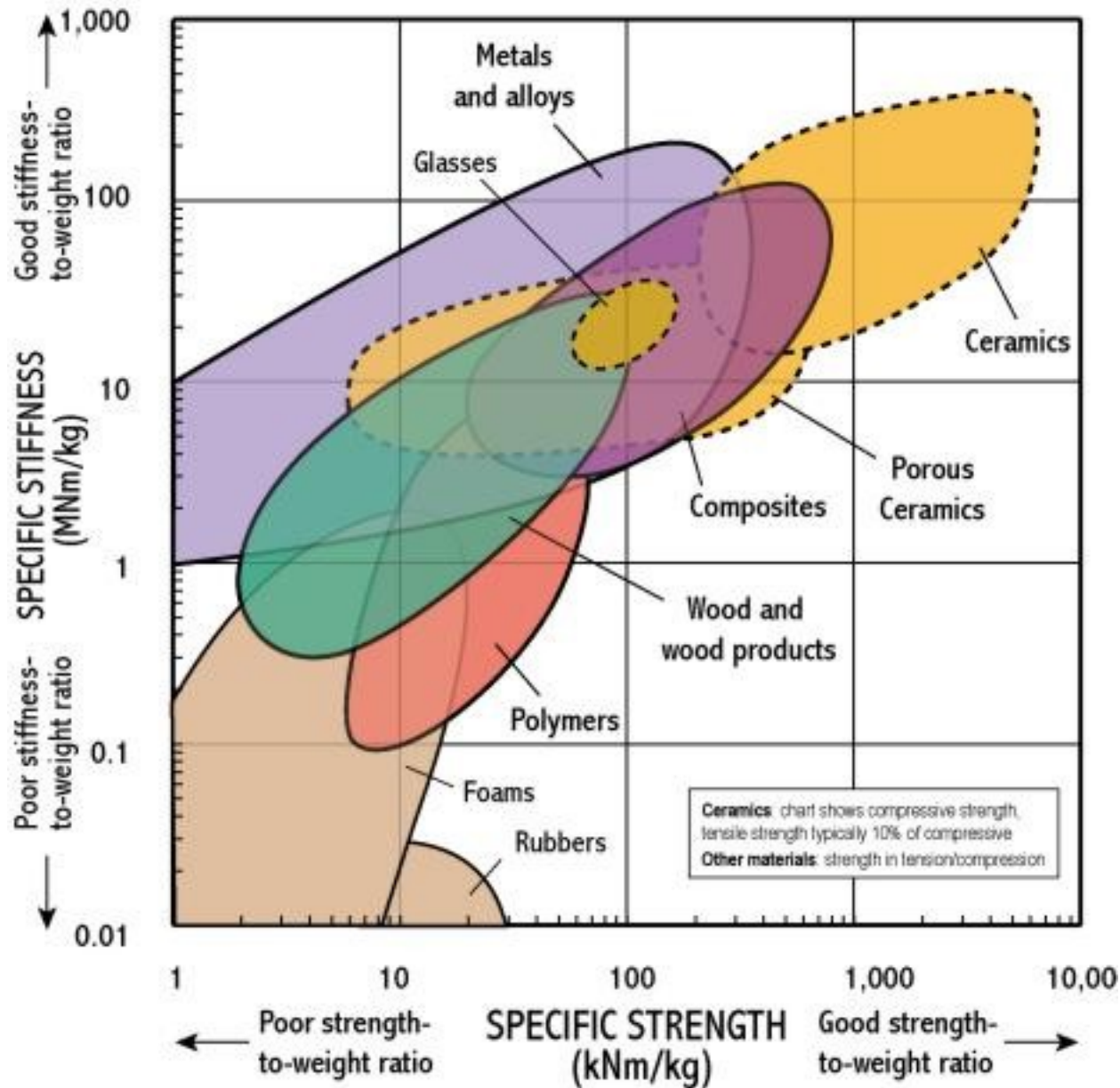


- Image courtesy: Chinese National Science Foundation webpage
- Rate of straining is important!
- Slow strain rates so that system can adjust

# Strength-Density chart



# Stiffness—Strength (specific) chart

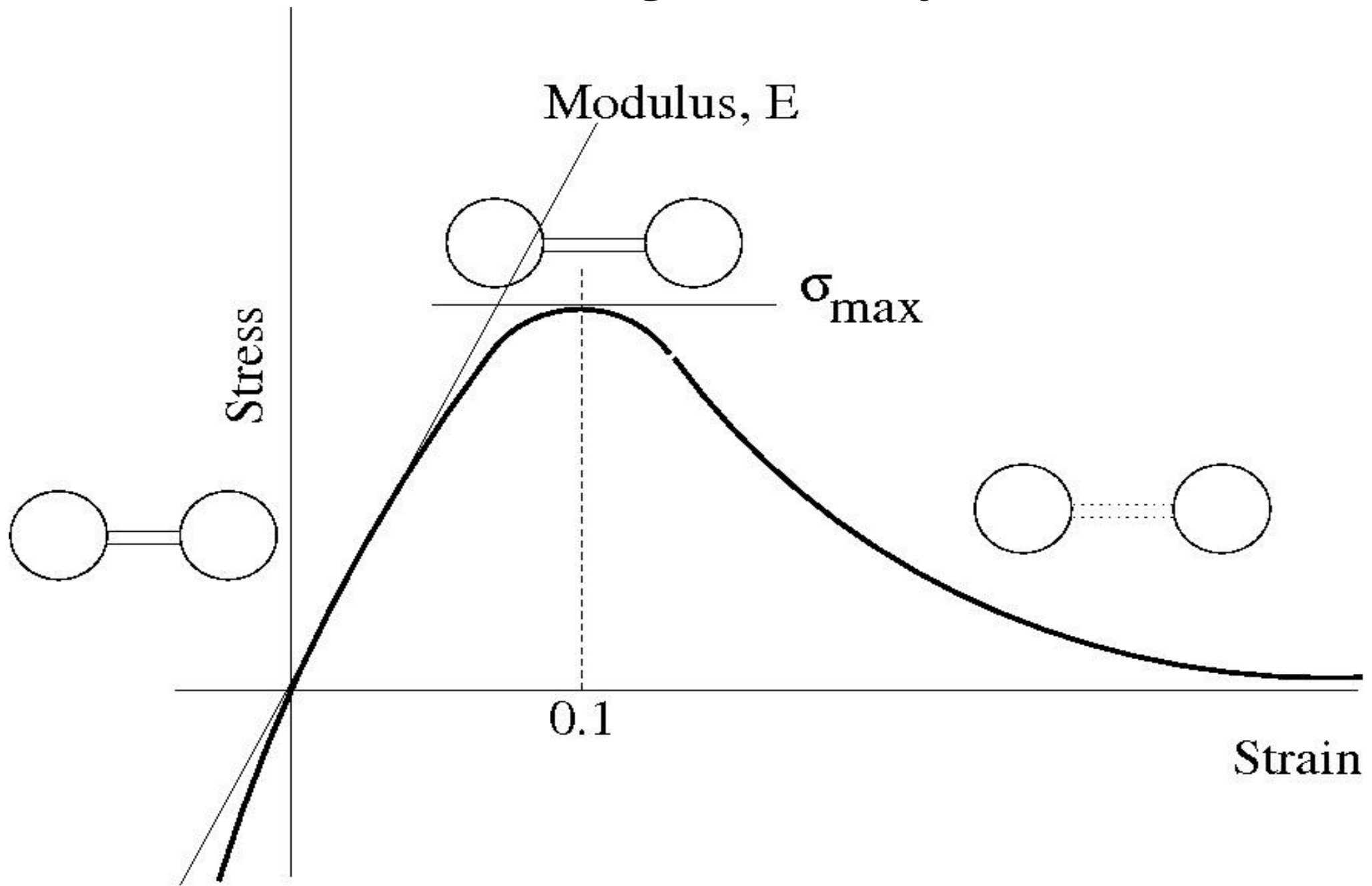


# Ideal strength of crystals

- Atoms in a crystal – connected via bonds (springs)
- The springs have a breaking point!
- Connect the breaking point with the material constant – namely, modulus!



# Ideal strength of crystals



# Ideal strength of crystals

- Let the strain at which the bond is broken be 0.1
- Let the initial interatomic distance be “a”
- The force needed to break the bond is then (roughly)  $Sa/10$
- $S$  – bond stiffness
- The ideal strength is then
$$\sigma_{max} = Sa/10a^2 = S/10a = E/10$$
- More refined estimate (including curvature of force-distance curve):  $E/15$

# Theory versus practice

In theory, there is no difference between theory and practice. But, in practice, there is.

-- Attributed to Jan L. A. van de Snepscheut/Yogi Berra

# Observed versus theoretical

- Copper:  
Yield strength: 70 M Pa  
Young's modulus: 110-130 G Pa
- Aluminium alloy:  
Yield strength: 400 M Pa  
Young's modulus: 69 G Pa

# Why the discrepancy?

Defects!